

# 1.5 Infinite Geometric Series

## Infinite Geometric Series

Example:  $\frac{1}{2} + \frac{1}{4} + \frac{1}{8} + \frac{1}{16} + \dots$

### Idea of Partial Sum

add the first two terms, the first three terms, and so on.

$$S_1 = \frac{1}{2}$$

$$S_2 =$$

$$S_3 =$$

$$S_4 =$$

Are the partial sums approaching a particular value? Confirm answer using the formula.

### ***Convergent Geometric Series:***

- a series with an infinite number of terms, in which the sequence of partial sums approaches a fixed value
- occurs when  $-1 < r < 1$

### ***Divergent Geometric Series:***

- a series with an infinite number of terms, in which the sequence of partial sums does not approach a fixed number

***Distinguish between a convergent and divergent series***

Geometric Series	Ratio (r)	Partial Sum	Convergent/ Divergent
$2+4+8+16\dots$			
$\frac{1}{2} + \frac{1}{4} + \frac{1}{8} + \frac{1}{16} + \dots$			
$-1+1+-1+1+\dots$			
$1+1+1+1+\dots$			

If the partial sums **approach a particular value** as the number of terms get larger, the series is convergent.

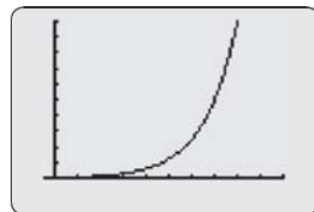
If the partial sums **do not approach a particular value** the series is divergent.

**Example:** Consider the series:  $4 + 8 + 16 + 32 + \dots$

$$\begin{aligned} S_1 &= 4 \\ S_2 &= 12 \\ S_3 &= 28 \\ S_4 &= 60 \\ S_5 &= 124 \end{aligned}$$



X	Y1
1	4
2	12
3	28
4	60
5	124
6	252
7	508
8	1020



As the number of terms increases, the sum of the series \_\_\_\_\_

**Example:** Consider the series:  $\frac{3}{2} + \frac{3}{4} + \frac{3}{8} + \frac{3}{16} + \dots$

$$S_1 =$$

$$S_2 =$$

$$S_3 =$$

$$S_4 =$$

As the number of terms increases, the sum of the series approaches \_\_\_\_\_ ?

**Infinite Geometric Series:**

$$S_\infty = \frac{t_1}{1-r}, \text{ where } -1 < r < 1$$

Example 2: Your Turn

Determine whether each infinite geometric series converges or diverges.

Calculate the sum, if it exists.    **a)**  $1 + \frac{1}{5} + \frac{1}{25} + \dots$                       **b)**  $4 + 8 + 16 + \dots$

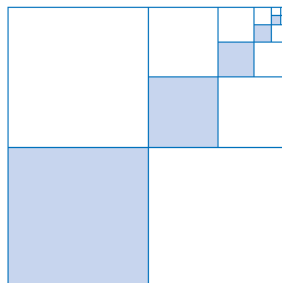
Example 3: Your Turn

You can express  $\overline{0.584}$  as an infinite geometric series.  
 $\overline{0.584} = 0.584\ 584\ 584\ \dots$   
 $\quad = 0.584 + 0.000\ 584 + 0.000\ 000\ 584 + \dots$   
 Determine the sum of the series.

Example 4: Apply the Sum of an Infinite Geometric Series

Assume that each shaded square represents  $\frac{1}{4}$  of the area of the larger square bordering two of its adjacent sides and that the shading continues indefinitely in the indicated manner.

- a) Write the series of terms that would represent this situation.
- b) How much of the total area of the largest square is shaded?



Key Ideas p. 63

Assign p.63-65

1(b), 2(abd), 3(a), 4, 5(ac), 6, 7, 8, 9, 12, 13, 15, 17, 22