

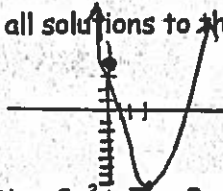
Mathematics 20-1
 Chapter 4: Quadratic Equations
 Final Exam Review Assignment

Name: Answers
 Date: _____

Quadratic Formula: $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$

1. Solve $0.5x^2 - 3x = 4$ by graphing. Round all solutions to the nearest tenth.

$0.5x^2 - 3x - 4 = 0$
 vertex $\frac{3}{2(0.5)} = 3$
 $0.5(3)^2 - 3(3) - 4 = -8.5$



2. Determine the exact roots to the equation $2x^2 = 5x + 3$ using technology.

$2x^2 - 5x - 3 = 0$ $\begin{array}{r} p - b \\ 5 - 5 \\ \hline -6 \end{array}$ $2x + 1 = 0$ $x - 3 = 0$
 $2x^2 - 6x + x - 3 = 0$ $\begin{array}{r} -6 \end{array}$ $x = -\frac{1}{2}$ $x = 3$
 $2x(x-3) + (x-3) = 0$

3. Factor each of the following completely.

a) $(x+3)^2 + 2(x+3) - 24$ Let $m = x+3$
 $m^2 + 2m - 24$ $\begin{array}{r} p - 24 \\ 5 \quad 2 \\ \hline 6 \quad -4 \end{array}$
 $= (m+6)(m-4)$
 $= (x+3+6)(x+3-4)$
 $= (x+9)(x-1)$

b) $2(4x-1)^2 + 9(4x-1) + 10$ Let $m = 4x-1$
 $2m^2 + 9m + 10$ $\begin{array}{r} p 20 \\ 5 \quad 9 \\ \hline 4 \quad 5 \end{array}$
 $= 2m^2 + 4m + 5m + 10$
 $= 2m(m+2) + 5(m+2)$
 $= (2m+5)(m+2)$
 $= (2(4x-1)+5)(4x-1+2)$
 $= (8x-2+5)(4x+1)$
 $= (8x+3)(4x+1)$

4. Solve each quadratic equation by factoring.

a) $2a^2 - 10a - 28 = 0$
 $2(a^2 - 5a - 14) = 0$
 $2(a-7)(a+2) = 0$
 $a-7 = 0$ $a+2 = 0$
 $a = 7$ $a = -2$

b) $10b^2 + 13b = 3$
 $10b^2 + 13b - 3 = 0$ $\begin{array}{r} p - 30 \\ 5 \quad 13 \\ \hline -15 \quad 2 \end{array}$
 $5b(2b-3) + 1(2b-3) = 0$
 $(5b+1)(2b-3) = 0$
 $5b+1 = 0$ $2b-3 = 0$
 $b = -\frac{1}{5}$ $b = \frac{3}{2}$

c) $16p^2 - 9 = 0$
 $(4p-3)(4p+3) = 0$
 $4p-3 = 0$ $4p+3 = 0$
 $p = \frac{3}{4}$ $p = -\frac{3}{4}$

d) $6x^2 + 4 = 11x$
 $6x^2 - 11x + 4 = 0$ $\begin{array}{r} p 24 \\ 5 - 11 \\ \hline -5 \quad -3 \end{array}$
 $6x^2 - 8x - 3x + 4 = 0$
 $2x(3x-4) - 1(3x-4) = 0$
 $(2x-1)(3x-4) = 0$
 $2x-1 = 0$ $3x-4 = 0$
 $x = \frac{1}{2}$ $x = \frac{4}{3}$

5. Use the quadratic formula to solve each quadratic equation. Express answers as exact values in simplest form.

a) $3x^2 - 6x + 1 = 0$

$$x = \frac{6 \pm \sqrt{(-6)^2 - 4(3)(1)}}{2(3)}$$

$$x = \frac{6 \pm \sqrt{36 - 12}}{6}$$

$$x = \frac{6 \pm \sqrt{24}}{6}$$

$$x = \frac{6 \pm 2\sqrt{6}}{6}$$

$$x = \frac{3 \pm \sqrt{6}}{2}$$

b) $4x^2 = 3 - 10x$

$$4x^2 + 10x - 3 = 0$$

$$x = \frac{-10 \pm \sqrt{10^2 - 4(4)(-3)}}{2(4)}$$

$$x = \frac{-10 \pm \sqrt{100 + 48}}{8}$$

$$x = \frac{-10 \pm \sqrt{148}}{8}$$

$$x = \frac{-10 \pm 2\sqrt{37}}{8}$$

$$x = \frac{-5 \pm \sqrt{37}}{4}$$

6. Solve each of the following quadratic equations. Give solutions as exact values, in simplest form.

a) $16x^2 - 8x + 1 = 0$

$\begin{matrix} p & 16 \\ q & -8 \\ r & 1 \end{matrix}$

$$16x^2 - 4x - 4x + 1 = 0$$

$$4x(4x-1) - 1(4x-1) = 0$$

$$(4x-1)(4x-1) = 0$$

$$4x-1=0 \quad 4x-1=0$$

$$x = \frac{1}{4}$$

$$x = \frac{1}{4}$$

b) $2x^2 + 1 = 6x$

$$2x^2 - 6x + 1 = 0$$

$$x = \frac{6 \pm \sqrt{(-6)^2 - 4(2)(1)}}{2(2)}$$

$$x = \frac{6 \pm \sqrt{36 - 8}}{4}$$

$$x = \frac{6 \pm \sqrt{28}}{4}$$

$$x = \frac{6 \pm 2\sqrt{7}}{4}$$

$$x = \frac{3 \pm \sqrt{7}}{2}$$